

# Long-Lived Particles (LLP) and Displaced Vertices

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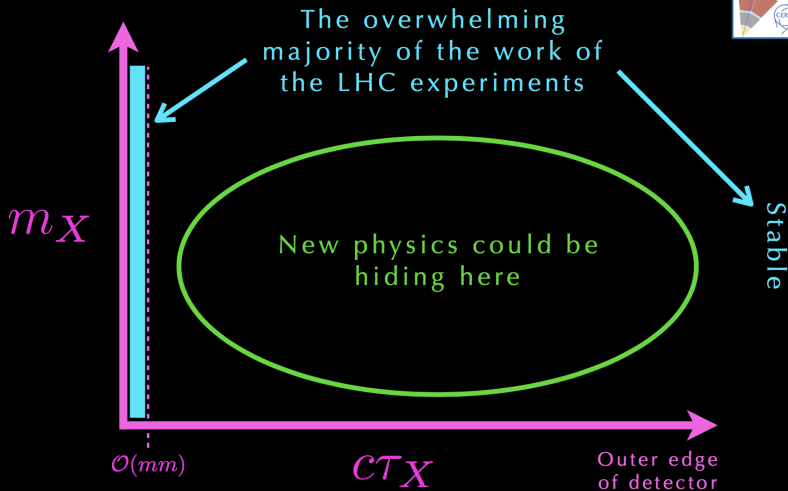
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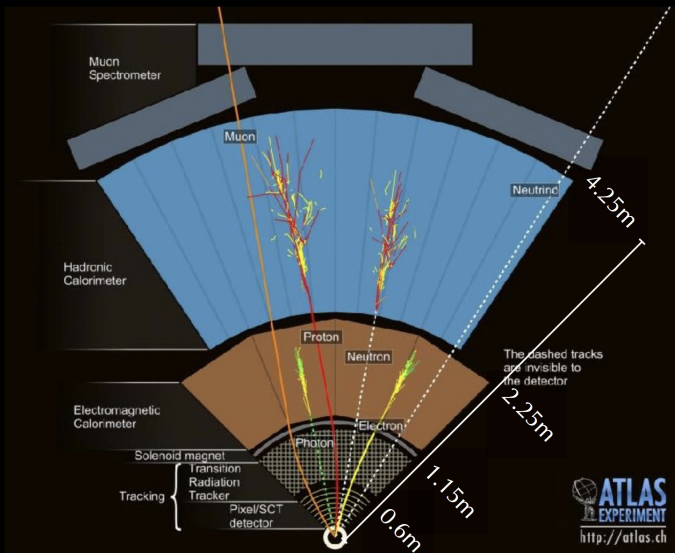
**Are we looking at the right places?**

# What IF?

# New physics $X$ at the LHC



95% of our analysis effort is dedicated to understanding five prompt objects





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Most importantly: Motivations, Predictability and Detectability!

The question then is why we have not seen any new physics signals yet if they are there. The answer to the aforementioned question might be the possibility that we have "missed" new physics signals due to the fact that most experimental search algorithms focus mainly at prompt decays with decay lengths less than 1 mm and at stable particles. Long-lived particles (LLP) can be defined as (BSM) particles which decay into SM particles or give up all their energies inside the detector acceptance of the present LHC detectors LHCb, CMS, ATLAS as well as the proposed detectors MilliQan, MoEDAL, MATHUSLA, etc...Experimentalists and theorists got together recently to form The LHC LLP Community, a CERN initiative, which is growing and which hold regular workshops

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Giant Isopod



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CLEARLY THE ONLY EVIDENCE  
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neutrino masses: seesaw mechanism

$$m_\nu = m_D^2 / M_R \text{ with}$$

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Where are they?

Do they interact with  $W$ 's and  $Z$  or not?

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**Why should they be so???**



# What IF?

Right-handed neutrinos are **non-sterile**. They interact with  $W$  and  $Z$ . Their masses  $M_R$  are proportional to  $\Lambda_{EW} \sim 246 \text{ GeV}$ .

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- **Experimental**: They are "light" (LHC-accessible) and have typical electroweak production cross sections  $\Rightarrow$  Direct test of seesaw.

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- Theoretical: Deep connection between neutrino masses and the strong CP problem, among others. With mirror fermions, one can now study EW phase transitions non-perturbatively on a lattice: Important for cosmology!
- How does one construct a model in which  $M_R \propto \Lambda_{EW} \sim 246 \text{ GeV}$  with  $\nu_R$  carrying SM quantum numbers?

## Lee and Yang on Parity Violation:

"If such asymmetry is indeed found, the question could still be raised whether there could not exist corresponding elementary particles exhibiting opposite asymmetry such that in the broader sense there will still be over-all right-left symmetry.."

PR104, 254, October 1956.



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- $M_R \propto \Lambda_{EW}$ ? From the VEV of a triplet Higgs field  $\tilde{\chi} = (\chi^0, \chi^+, \chi^{++})$  and lepton-number violating mass term

$$L_M = g_M I_R^{M,T} \sigma_2 \tau_2 \tilde{\chi} I_R^M.$$

# The EW- $\nu_R$ model

- With  $\langle \chi^0 \rangle = v_M < \Lambda_{EW}$ , right-handed neutrino Majorana mass  $M_R = g_M v_M \Rightarrow$   
 $M_Z/2 < M_R < O(\Lambda_{EW} \sim 246 \text{ GeV})$ :  
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- Wait! Isn't it too complicated? If  $M_R$  comes from **symmetry breaking**, it's **unavoidable** to have a Higgs structure larger than that of the SM. E.g. **126** of **SO(10)** or a **triplet  $\Delta_R$**  of **L-R model**.



# The EW- $\nu_R$ model

•  $m_D?$

# The EW- $\nu_R$ model

- $m_D$ ? From the VEV of a **complex singlet Higgs field**  $\phi_S$ . Lepton-number conserving term  $\mathcal{L}_S = -g_{SI} \bar{l}_L \phi_S l_R^M + \text{H.c.}$   
 $m_D = g_{SI} v_S$  where  $\langle \phi_S \rangle = v_S$ . Crucial in the discussion of the phenomenology of the model and the strong CP problem

# The EW- $\nu_R$ model

- $I_R^M = \begin{pmatrix} \nu_R^M \\ e_R^M \end{pmatrix}$ : Anomaly cancellation  $\rightarrow$

Mirror quarks:  $q_R^M = \begin{pmatrix} u_R^M \\ d_R^M \end{pmatrix}$

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- Gauge group:  $SU(3)_C \times SU(2)_W \times U(1)_Y$ . Notice the subscript  $W$  instead of  $L$ .

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- Scalars:

\* **Doublet Higgs fields (similar to 2HDM)**:  $\Phi_1^{SM}(Y/2 = -1/2)$ ,  $\Phi_2^{SM}(Y/2 = +1/2)$  coupled to SM fermions, and  $\Phi_1^M(Y/2 = -1/2)$ ,  $\Phi_2^M(Y/2 = +1/2)$  coupled to mirror fermions with  $\langle \Phi_1^{SM} \rangle = (v_1/\sqrt{2}, 0)$ ,  $\langle \Phi_2^{SM} \rangle = (0, v_2/\sqrt{2})$  and  $\langle \Phi_1^M \rangle = (v_1^M/\sqrt{2}, 0)$ ,  $\langle \Phi_2^M \rangle = (0, v_2^M/\sqrt{2})$ .

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\*Triplet Higgs fields:

$$\chi = \begin{pmatrix} \chi^0 & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^{0*} \end{pmatrix}$$

$\xi$  ( $Y/2 = 0$ ) =  $(\xi^+, \xi^0, \xi^-)$  with  $\langle \chi^0 \rangle = \langle \xi^0 \rangle = v_M$  in order to preserve  
Custodial Symmetry (that guarantees  $M_W^2 = M_Z^2 \cos^2 \theta_W$  at tree level.

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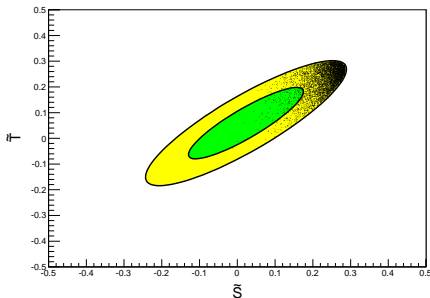
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\*So many Higgs fields? Nothing to be afraid of. Good hunting ground!

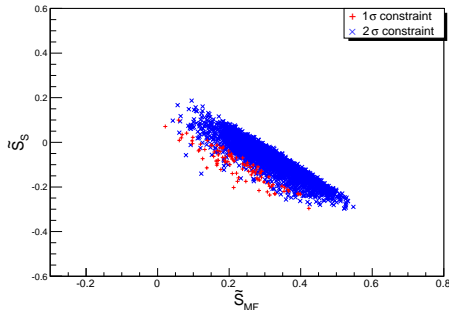
# Summary of the EW- $\nu_R$ model: Precision constraints

Fig. 1 and 2 are the  $1\sigma$  and  $2\sigma$  constraints.  $\tilde{T}$  and  $\tilde{S}$  are the total contributions (mirror fermions plus scalars) after subtracting out the SM contributions.



# Summary of the EW- $\nu_R$ model: Precision constraints

$\tilde{S}_S$  and  $\tilde{S}_{MF}$  are the contributions to  $S$  from the scalars (mainly the triplets) and the mirror fermions.



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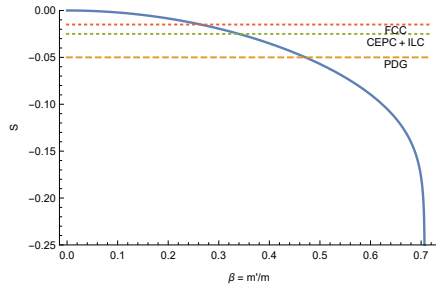
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- 2016 PDG value for  $\tilde{S} = 0.07 \pm 0.08$
- Notice that, for a large range of parameters, the contribution to  $\tilde{S}$  from Triplet scalars is generally negative and large (see the previous figure)!
- If only triplet scalar is present  $\Rightarrow$  very small region of parameter space for  $\tilde{S}$  is allowed  $\Rightarrow$  fine-tuning problem! The much larger parameter space which allows mass splitting inside the triplet has large and negative values for  $\tilde{S}$  which need to be cancelled by similar positive amount coming from another sector such as the mirror fermion sector! One cannot play around with triplet Higgs without experimental consequences!



**Figure:**  $S$  vs the mass splitting ratio  $\beta = \frac{m'}{m}$ . The dashed and the dotted lines represent the current precision (PDG) and the projected precision for the ILC and CEPC colliders.

## Summary of the EW- $\nu_R$ model: 125-GeV scalar

There are many choices of parameters which can accommodate the 125-GeV scalar. Some are more SM-like, some are not.

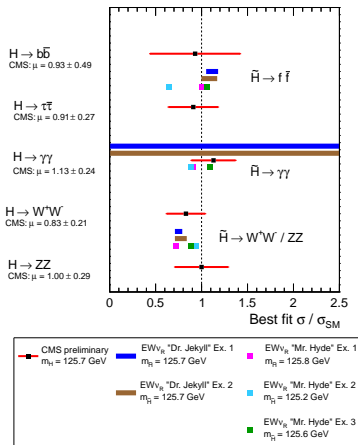


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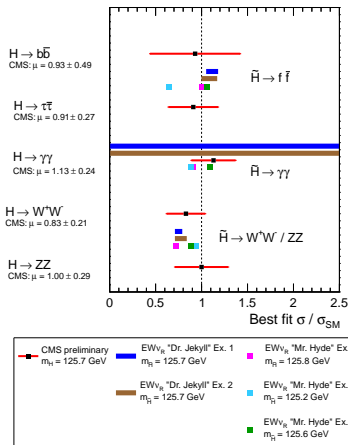
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Some examples on the next slide

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We need to  
 measure the  
 partial widths  
 to know the  
 true nature  
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 125-GeV!  
 Higgs  
 factory?  
 Unless...

# Search for mirror fermions: Characteristic signatures

Two **important characteristic signatures** to pay attention to in the search for  $\nu_R$ 's and **accompanying mirror fermions**.

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I) Lepton-number violating signals at high energy: Like-sign dileptons from the decays of  $\nu_R \nu_R$  ( $q\bar{q} \rightarrow Z \rightarrow \nu_R \nu_R$ ) . Remember  $\nu_R$ : Majorana!

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- The appearance of **like-sign dileptons**  
 $(e^-e^-, \mu^-\mu^-, \tau^-\tau^-, e^-\mu^-, \dots)$  could be at **displaced vertices**.

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- $q_R^M \rightarrow q_L + \phi_S$ : The decay length will depend on the Yukawa couplings  $g_{Sq}$ . Unlike the mirror lepton cases, there are no direct or indirect experimental constraints  $g_{Sq}$ .



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- Constraint on  $\bar{\theta} \Rightarrow$  Constraint on  $g_{Sq} < g_{SI} \Rightarrow$  Displaced vertices in mirror quark decays.

# $g_{Sq}$ constraint from the strong CP problem

- The vacuum of QCD is complicated. 't Hooft: The proper gauge-invariant vacuum is characterized by an "angle"

$$|\theta\rangle = \sum_n \exp(-in\theta) |n\rangle$$

$$\Rightarrow S_{eff} = S_{gauge} + \theta_{QCD} (g_3^2/32\pi^2) \int d^4x G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a$$

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- $\theta_{\text{QCD}} < 10^{-10}$ . Why is it so small? That is the strong CP problem.

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- **How small?**

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- The essence of the axionless solution can be found with a toy model of one family. A generalization to three families can be carried out.



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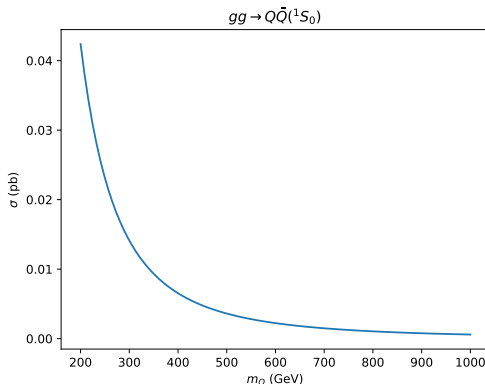
# Search for mirror quarks

$q_R^M \rightarrow q_L + \phi_S$ . Example::

Typical decay length  $\gg$   
Hadronization length  
 $\sim O(1\text{fermi})$

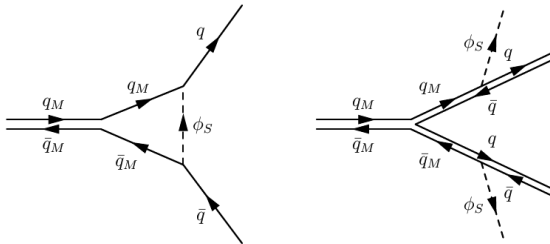
Formation of QCD bound states

Mirror mesons:  $\bar{q}^M q^M$  and Hybrid  
mesons  $\bar{q}^M q$  get formed first  
before they decay!



# Search for mirror quarks

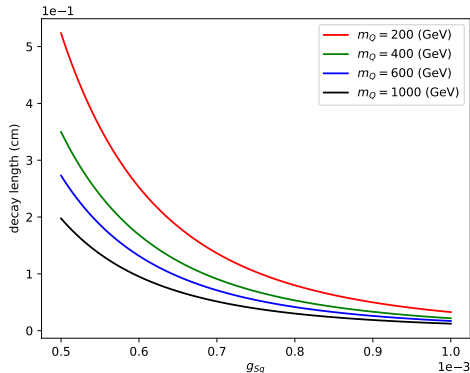
## Mirror-meson decays



# Search for mirror quarks

Mirror-meson decay lengths:

Displaced Vertices  $> O(cm)$  for  $g_{Sq} < 10^{-4}$ .



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- There seems to be a **deep connection** between **neutrino physics** and **QCD** in the solution to the strong CP problem.
- **Nielsen-Ninomiya theorem**: The EW-scale  $\nu_R$  model evades the N-N theorem and one can now study EW phase transition on the lattice.
- If space is indeed discrete at the Planck scale then the Nielsen-Ninomiya no-go theorem requires the existence of mirror fermions. Deep implications for Quantum Gravity?

And...

Mucho gracias fefo por una  
conferencia maravillosa!

And...

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Viva Tequila!

Keep in mind...

# New Physics with Exotic and Long-lived Particles: A joint ICISE-CBPF Symposium

July 1-6, 2019, Quy Nhon, Vietnam



# Some papers

- EW-scale  $nu_R$  model; PQH, Phys. Lett. B **649**, 275 (2007).
- EW precision: V. Hoang, P. Q. Hung and A. S. Kamat, Nucl. Phys. B **877**, 190 (2013) doi:10.1016/j.nuclphysb.2013.10.002 [arXiv:1303.0428 [hep-ph]].
- 125-GeV scalar: V. Hoang, P. Q. Hung and A. S. Kamat, Nucl. Phys. B **896**, 611 (2015) doi:10.1016/j.nuclphysb.2015.05.007 [arXiv:1412.0343 [hep-ph]].
- Rare decays: P. Q. Hung, T. Le, V. Q. Tran and T. C. Yuan, JHEP **1512**, 169 (2015) doi:10.1007/JHEP12(2015)169 [arXiv:1508.07016 [hep-ph]].



## Some papers

- Searches: S. Chakdar, K. Ghosh, V. Hoang, P. Q. Hung and S. Nandi, Phys. Rev. D **93**, no. 3, 035007 (2016) doi:10.1103/PhysRevD.93.035007 [arXiv:1508.07318 [hep-ph]], S. Chakdar, K. Ghosh, V. Hoang, P. Q. Hung and S. Nandi, Phys. Rev. D **95**, no. 1, 015014 (2017) doi:10.1103/PhysRevD.95.015014 [arXiv:1606.08502 [hep-ph]].
- **strong CP**: arXiv:1704.06390 [hep-ph]; **mirror fermion searches**: Phys. Lett. B **649**, 275 (2007); Phys. Rev. D **95**, no. 1, 015014 (2017); Phys. Rev. D **93**, no. 3, 035007 (2016),...
- More are in preparation.

# Backup slides

- Peccei and Quinn solution:  
Extra global symmetry  $U(1)_{PQ}$  (chiral)
- P-Q Toy model: Single flavor  $\psi$  interacting with a scalar  $\phi$ ; Chiral symmetry  $U(1)_A$  (or  $U(1)_{PQ}$ ). Lagrangian invariant under a chiral rotation  
 $\psi \rightarrow \exp(i\sigma\gamma_5)\psi$ ;  $\phi \rightarrow \exp(-i2\sigma)\phi$
- Jackiw-Rebbi:  $\theta_{QCD} \Rightarrow \theta_{QCD} - 2\sigma \Rightarrow$  All vacua are equivalent  $\Rightarrow$  one can rotate  $\theta_{QCD}$  to zero! No CP violation!
- Peccei and Quinn have proved that 1)  $\langle\phi\rangle = 0 \Rightarrow$  No CP violation; 2) even if  $\langle\phi\rangle \neq 0$  No CP violation if  $\bar{\theta}$  is replaced by an axion field  $a(x)$  where the minimum of an (quite complicated) effective potential is where the effective  $\theta$  is zero.
- Visible axion ruled out by beam dump experiment. Invisible axion not found after more than 30 years or so.

# The strong CP problem: Brief review

- There are several **axionless** models for the strong CP problem:  
Nelson, Barr,...

# Neutrinos and the strong CP problem

Ingredients of the EW- $\nu_R$  model which help solve the strong CP problem without an axion.

- Mirror fermions.
- Mixing of mirror with SM fermions  $\Rightarrow$  Dirac mass of neutrinos through  $g_{SI} \bar{l}_L \phi_S l_R^M$ .
- A global symmetry  $U(1)_{SM} \times U(1)_{MF}$  was imposed to prevent terms such as  $\bar{l}_L \tilde{\chi} l_R^M$  (Dirac mass too big);  $l_L^T \sigma_2 \tau_2 \tilde{\chi} l_L$  (gives rise to unwanted  $\nu_L^T \nu_L$ ),...which spoil the seesaw mechanism.

What do the above ingredients have to do with the strong CP problem?

# Neutrinos and the strong CP problem

- Most of salient points concerning the solution to the strong CP problem can be obtained with a toy model with one family.

- Relevant Yukawa interactions

$$\mathcal{L}_{mass} = g_u \bar{q}_L \Phi_1^{SM} u_R + g_d \bar{q}_L \Phi_2^{SM} d_R + g_u^M \bar{q}_R^M \Phi_1^M u_L^M + g_d^M \bar{q}_R^M \Phi_2^M d_L^M + H.c.,$$

$$\mathcal{L}_{mixing} = g_{Sq} \bar{q}_L \phi_S q_R^M + g_{Su} \bar{u}_L^M \phi_S u_R + g_{Sd} \bar{d}_L^M \phi_S d_R + H.c..$$

- Step 1 of the solution to strong CP (Peccei-Quinn): Use a chiral symmetry to rotate away  $\theta_{QCD}$ .

$\mathcal{L}_{mixing}$  and  $\mathcal{L}_{mass}$  are invariant under:  $q \rightarrow \exp(i\alpha_{SM}\gamma_5)q$ ;  $q^M \rightarrow \exp(i\alpha_{MF}\gamma_5)q^M$ ;  $\phi_S \rightarrow \exp(-i(\alpha_{SM} + \alpha_{MF}))\phi_S$  under the chiral symmetries  $U(1)_{A,SM} \times U(1)_{A,MF}$  contained in  $U(1)_{SM} \times U(1)_{MF}$ . Jackiw-Rebbi:  $\theta_{QCD} \rightarrow \theta_{QCD} - (\alpha_{SM} + \alpha_{MF})$

- All vacua are equivalent and one can choose the CP-conserving vacuum  $\theta_{QCD} - (\alpha_{SM} + \alpha_{MF}) = 0$ .

# Neutrinos and the strong CP problem

- Notice that  $g_u$ ,  $g_d$ ,  $g_u^M$ ,  $g_d^M$ ,  $g_{Sq}$ ,  $g_{Su}$  and  $g_{Sd}$  can, in general be complex. If we absorb the phases into  $u_R$ ,  $u_L^M$ ,  $d_R$  and  $d_L^M$  to make the *diagonal* elements of the  $(2 \times 2)$  up and down mass matrices *real* then the *off-diagonal* elements stay *complex*.

$$\mathcal{M}_u = \begin{pmatrix} m_u & |g_{Sq}|v_S \exp(i\theta_q) \\ |g_{Su}|v_S \exp(i\theta_u) & M_u \end{pmatrix} \quad (1)$$

$$\mathcal{M}_d = \begin{pmatrix} m_d & |g_{Sq}|v_S \exp(i\theta_q) \\ |g_{Sd}|v_S \exp(i\theta_d) & M_d \end{pmatrix} \quad (2)$$

# Neutrinos and the strong CP problem

- Step 2 of the solution to the strong CP problem: Calculation of  $\text{ArgDet} \mathcal{M}_u \mathcal{M}_d$ . Call that  $\theta_{\text{weak}}$ .

- $$\theta_{\text{Weak}} \approx -(r_u \sin(\theta_q + \theta_u) + r_d \sin(\theta_q + \theta_d))$$

$$r_u = \frac{|g_{Sq}| |g_{Su}| v_S^2}{m_u M_u} = \left( \frac{|g_{Sq}| |g_{Su}|}{g_{SI}^2} \right) \left( \frac{m_D^2}{m_u M_u} \right)$$

$$r_d = \frac{|g_{Sq}| |g_{Sd}| v_S^2}{m_d M_d} = \left( \frac{|g_{Sq}| |g_{Sd}|}{g_{SI}^2} \right) \left( \frac{m_D^2}{m_d M_d} \right)$$

$m_D = g_{SI} v_S$ : Dirac mass in seesaw.

$$m_\nu = m_D^2 / M_R$$

- Important remark:** Even with maximal CP phases  $\theta_q + \theta_{u,d} = \pi/2$ ,  $\theta_{\text{weak}} \rightarrow 0$  if  $r_{u,d} \rightarrow 0$ .
- Assuming  $g_{Sq}, g_{Su}, g_{Sd} \neq 0$ ,  $\theta_{\text{weak}} \rightarrow 0$  if  $v_S \rightarrow 0$  or  $m_\nu \rightarrow 0$ .
- Smallness of neutrino mass  $\Rightarrow$  smallness of  $\bar{\theta}$  !** No need to make  $\bar{\theta}$  zero.

# Neutrinos and the strong CP problem

- Putting in numbers

$$\theta_{Weak} < -10^{-8} \left\{ \left( \frac{|g_{Sq}||g_{Su}|}{g_{SI}^2} \right) \sin(\theta_q + \theta_u) + \left( \frac{|g_{Sq}||g_{Sd}|}{g_{SI}^2} \right) \sin(\theta_q + \theta_d) \right\}$$

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